a.

2

Essential Question How do you divide by a fraction?

ACTIVITY: Dividing by a Fraction Work with a partner. 1 $8 \div 16$ Describe the pattern of the blue numbers. $\overline{2}$ **b.** Describe the pattern of the red numbers. 1 8 ÷ 8 Use the pattern to complete the table. 2 **c.** The division $8 \div \frac{1}{2}$ can be read as "How many halves 8 ÷ 4 4 8 ÷ 2 are in 8?" Use the completed table to answer this question. Then draw a model that shows your answer. 8 $8 \div 1$ **d.** Use the pattern in the table to complete the following. $\frac{1}{2}$ 8 ÷ $8 \div \frac{1}{2} = 16 = 8 \times \frac{2}{1}$ Invert $\frac{1}{2}$ and multiply. $\frac{1}{4}$ 8 ÷ $8 \div \frac{1}{4} = 32 =$ $\frac{1}{8}$

ACTIVITY: Dividing by a Fraction

Work with a partner.

 $8 \div \frac{1}{8} = 64 =$

a. Draw a model for $3 \div \frac{2}{3}$. Use the model to answer the question "How many two-thirds are in 3?"



b. Complete the table in two ways. First use the model. Then use the "invert and multiply" rule that you found in Activity 1. Compare your answers.

$3 \div \frac{2}{3}$	
$6 \div \frac{2}{3}$	
$9 \div \frac{2}{3}$	
$12 \div \frac{2}{3}$	

8 ÷

ACTIVITY: Dividing by a Fraction

3

Work with a partner. Write the division problem and answer it using a model.

a. How many halves are in five halves?



b. How many sixths are in three halves?



c. How many three-fourths are in 3?



d. How many four-fifths are in 8?



e. How many three-tenths are in 6?



f. How many halves are in a fourth?



-What Is Your Answer?

4. IN YOUR OWN WORDS How do you divide by a fraction? Give an example.



Use what you learned about dividing fractions to complete Exercises 11–18 on page 75.

2.5 Lesson





Two numbers whose product is 1 are **reciprocals**. To write a reciprocal of a number, write the number as a fraction. Then invert the fraction.

The Meaning of a Word Invert

When you **invert** a glass, you turn it over.



EX	AN	ЛР	LE

1

Writing Reciprocals

Study Tip 🦯	
When any number is multiplied by 0, the product is 0. So, the number 0 does not have a reciprocal.	

	Original Number	Fraction	Reciprocal	Check
a.	$\frac{3}{5}$	$\frac{3}{5}$	$\frac{5}{3}$	$\frac{3}{5} \times \frac{5}{3} = 1$
b.	$\frac{9}{5}$	$\frac{9}{5}$	$5\frac{5}{9}$	$\frac{9}{5} \times \frac{5}{9} = 1$
c.	2	$\frac{2}{1}$	$\frac{1}{2}$	$\frac{2}{1} \times \frac{1}{2} = 1$

On Your Own

Write the reciprocal of the number.



1. $\frac{3}{4}$ **3.** $\frac{7}{2}$ **4.** $\frac{4}{9}$ **2.** 5

0 Key Idea

Dividing Fractions

Words To divide a number by a fraction, multiply the number by the reciprocal of the fraction.

Numbers $\frac{1}{5} \div \frac{3}{4} = \frac{1}{5} \times \frac{4}{3}$ Algebra $\frac{a}{b} \div \frac{c}{d} = \frac{a}{b} \times \frac{d}{c}$, where *b*, *c*, and $d \neq 0$



EXAMPLE 3 Dividing a Whole Number by a Fraction

3

<u>3</u> 4

<u>3</u> 4

<u>3</u> 4

1 ft

2 ft

3 ft

A piece of wood is 3 feet long. How many $\frac{3}{4}$ -foot pieces can be cut from the piece of wood?

Method 1: Draw a diagram. Mark each foot on the diagram. Then divide each foot into $\frac{1}{4}$ -foot sections.

Count the number of $\frac{3}{4}$ -foot pieces of wood. There are four.

So, four $\frac{3}{4}$ -foot pieces can be cut from the piece of wood.

Method 2: Divide 3 by $\frac{3}{4}$ to find the number of $\frac{3}{4}$ -foot pieces.

 $3 \div \frac{3}{4} = 3 \times \frac{4}{3}$ Multiply by the reciprocal of $\frac{3}{4}$, which is $\frac{4}{3}$. $= \frac{1}{\cancel{3}} \frac{\cancel{3}}{\cancel{1}}$ Multiply. Divide out the common factor 3. = 4Simplify.

So, four $\frac{3}{4}$ -foot pieces can be cut from the piece of wood.

On Your Own

Now You're Ready Exercises 11–26 Divide. Write the answer in simplest form. 5. $\frac{2}{7} \div \frac{1}{3}$ 6. $\frac{1}{2} \div \frac{1}{8}$ 7. $\frac{3}{8} \div \frac{1}{4}$ 8. $\frac{2}{5} \div \frac{3}{10}$ 9. How many $\frac{1}{2}$ -foot pieces can be cut from a 7-foot piece of wood?

Evaluating an Algebraic Expression

Evaluate $a \div b$ when $a = \frac{4}{5}$ and b = 2.



🔵 On Your Own

EXAMPLE

Now You're Ready Exercises 32–35 4

Evaluate the expression $x \div y$ for the given values of x and y.

10. $x = \frac{1}{2}, y = 3$	11. $x = \frac{2}{3}, y = 10$
12. $x = \frac{5}{8}, y = 4$	13. $x = 4, y = \frac{1}{3}$

Using Order of Operations 5 **EXAMPLE** Evaluate $\frac{3}{9} + \frac{5}{6} \div 5$. $\frac{3}{8} + \frac{5}{6} \div \frac{5}{8} = \frac{3}{8} + \frac{5}{6} \times \frac{1}{5}$ Multiply by the reciprocal of 5, which is $\frac{1}{5}$. $= \frac{3}{8} + \frac{\cancel{5} \times 1}{6 \times \cancel{5}_1}$ Multiply $\frac{5}{6}$ and $\frac{1}{5}$. Divide out the common factor 5. $=\frac{3}{8}+\frac{1}{6}$ Simplify. $=\frac{9}{24}+\frac{4}{24}$ Rewrite fractions using the LCD 24. $=\frac{13}{24}$ Add. On Your Own Evaluate the expression. Now You're Ready Exercises 47–55 **14.** $\frac{4}{5} + \frac{2}{5} \div 4$ **15.** $\frac{3}{8} \div \frac{3}{4} - \frac{1}{6}$ **16.** $\frac{8}{9} \div 2 \div 8$







Write the reciprocal of the number.

1	7. 8	8. $\frac{6}{7}$	9. $\frac{2}{5}$	10. $\frac{8}{11}$
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Divide. Write the answer in simplest form.

2 3 11. $\frac{1}{8} \div \frac{1}{4}$	12. $\frac{5}{6} \div \frac{2}{7}$	13. $12 \div \frac{3}{4}$	14. $8 \div \frac{2}{5}$
15. $\frac{3}{7} \div 6$	16. $\frac{12}{25} \div 4$	17. $\frac{2}{9} \div \frac{2}{3}$	18. $\frac{8}{15} \div \frac{4}{5}$
19. $\frac{1}{3} \div \frac{1}{9}$	20. $\frac{7}{10} \div \frac{3}{8}$	21. $\frac{14}{27} \div 7$	22. $\frac{5}{8} \div 15$
23. $\frac{27}{32} \div \frac{7}{8}$	24. $\frac{4}{15} \div \frac{10}{13}$	25. $9 \div \frac{4}{9}$	26. $10 \div \frac{5}{12}$

ERROR ANALYSIS Describe and correct the error in finding the quotient.



29. **REASONING** How can you use estimation to show that the quotient in Exercise 28 is incorrect?

- **30.** APPLE PIE You have $\frac{3}{5}$ of an apple pie. You divide the remaining pie into five equal slices. What fraction of the original pie is each slice?
- 31. ANIMALS How many times longer is the baby alligator than the baby gecko?



- **57. NUMBER SENSE** When is the reciprocal of a fraction a whole number? Explain.
- **58. BUDGETS** The table shows the portions of a family budget that are spent on several expenses.
 - **a.** How many times more is the expense for housing than for automobiles?
 - **b.** How many times more is the expense for food than for recreation?
 - **c.** The expense for automobile fuel is $\frac{1}{60}$ of the total expenses. What fraction of the automobile expense is spent on fuel?

Expense	Portion of Budget
Housing	$\frac{1}{4}$
Food	$\frac{1}{12}$
Automobiles	$\frac{1}{15}$
Recreation	$\frac{1}{40}$



59.	GLAZING You have 6 pints of glaze. It takes $\frac{7}{8}$ pint
	to glaze a bowl and $\frac{9}{16}$ pint to glaze a plate.

- **a.** How many bowls could you glaze? How many plates could you glaze?
- **b.** You want to glaze 5 bowls and then use the rest for plates. How many plates can you glaze? How much glaze will be left over?
- **c.** How many of each object could you glaze so that there is no glaze left over? Explain how you found your answer.
- **60.** Reasoning: A water tank is $\frac{1}{8}$ full. The tank is $\frac{3}{4}$ full when 42 gallons of water are added to the tank.
 - **a.** How much water can the tank hold?
 - **b.** How much water was originally in the tank?
 - **c.** How much water is in the tank when it is $\frac{1}{2}$ full?

Fair Game Review what you learned in previous grades & lessons Estimate the quotient. (Section 2.1) 61. $12\frac{1}{9} \div 3\frac{4}{5}$ 62. $71\frac{2}{3} \div 8\frac{1}{4}$ 63. $90\frac{2}{7} \div 9\frac{3}{8}$ 64. $47\frac{3}{4} \div 7\frac{5}{6}$ 65. MULTIPLE CHOICE The expression 3m represents the cost of renting m movies. What is the cost of renting four movies? (Section 1.1) (A) \$7 (B) \$9 (C) \$12 (D) \$27